

1. Let  $\varepsilon$  denote the machine epsilon for the **Float64** format. If  $x \in \mathbf{R}$  is such that  $0 < x < \varepsilon$ , then  $x$  may or may not be representable in the **Float64** format.
2. Machine addition is commutative, meaning that  $a \hat{+} b = b \hat{+} a$  for any **Float64** point numbers  $a$  and  $b$ .
3. If  $x$  is a **Float64** and  $y$  is a **Float32** number, then the result of  $x + y$  is a **Float32** number.
4. The only polynomial  $p$  of degree at most 3 such that  $p(-1) = p(0) = p(1) = 0$  is the cubic polynomial  $p(x) = x^3 - x$ .
5. Given  $x_0 < x_1 < x_2$  and  $y_0, y_1, y_2 \in \mathbb{R}$ , the unique quadratic interpolating polynomial through these data points is given by

$$p(x) = \frac{(x - x_1)(x - x_2)}{(x_0 - x_1)(x_0 - x_2)}y_0 + \frac{(x - x_0)(x - x_2)}{(x_1 - x_0)(x_1 - x_2)}y_1 + \frac{(x - x_0)(x - x_1)}{(x_2 - x_0)(x_2 - x_1)}y_2.$$

6. Given  $x_0 < \dots < x_n$  and  $y_0, \dots, y_n \in \mathbb{R}$ , the constant polynomial  $p$  that minimizes  $\sum_{i=0}^n |y_i - p(x_i)|^2$  is given by

$$p(x) = \frac{1}{n+1} \sum_{i=0}^n y_i.$$

7. Let  $f(x) = \cos(2x)$ , and for any  $n \in \mathbb{N}$ , let  $f_n \in \mathcal{P}_n$  denote the polynomial interpolating  $f$  at  $n+1$  equidistant points  $-1 = x_0 < x_1 < \dots < x_n = 1$ . Then

$$\lim_{n \rightarrow \infty} \left( \max_{-1 \leq x \leq 1} |f(x) - f_n(x)| \right) = 0.$$

8. In Julia, if  $A$  is a matrix, then `A[:, iseven.(1:end)]` gives the matrix obtained by keeping only the columns with even indices.
9. The degree of precision of the Gauss–Legendre quadrature rule with  $n$  points is equal to  $2n - 1$ .
10. The degree of precision of the following integration rule is 3.

```
function I_approx(a, b, n)
    x = LinRange(a, b, n + 1)
    h = x[2] - x[1]
    return h * sum(f, x[1:n] .+ h/2)
end
```